## Latin squares and Cayley tables

Supplementary exercise. Below are all the Latin squares of size at most 5 (up to the relevant equivalence relation). In each case,
(a) Determine whether the given Latin square is the Cayley table of a group.
(b) If that's the case, give an example of a group whose Cayley table is the given Latin square.
(c) If that's not the case, give a reason why not.
(1)
(2)

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[1]
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(3)
$\left[\begin{array}{lll}1 & 2 & 3 \\ 2 & 3 & 1 \\ 3 & 1 & 2\end{array}\right]$
(5')
$\left[\begin{array}{llll}1 & 2 & 3 & 4 \\ 2 & 1 & 4 & 3 \\ 3 & 4 & 1 & 2 \\ 4 & 3 & 2 & 1\end{array}\right]$
$\left[\begin{array}{llll}1 & 2 & 3 & 4 \\ 2 & 4 & 1 & 3 \\ 3 & 1 & 4 & 2 \\ 4 & 3 & 2 & 1\end{array}\right]$
$\left[\begin{array}{lllll}1 & 2 & 3 & 4 & 5 \\ 2 & 3 & 5 & 1 & 4 \\ 3 & 5 & 4 & 2 & 1 \\ 4 & 1 & 2 & 5 & 3 \\ 5 & 4 & 1 & 3 & 2\end{array}\right]$
$\left[\begin{array}{lllll}1 & 2 & 3 & 4 & 5 \\ 2 & 4 & 1 & 5 & 3 \\ 3 & 5 & 4 & 2 & 1 \\ 4 & 1 & 5 & 3 & 2 \\ 5 & 3 & 2 & 1 & 4\end{array}\right]$

