Edward L. Green, Convex Algebras

This is joint work with Eduardo N. Marcos. Given a full subquiver \mathcal{L} of a quiver \mathcal{Q} and a K-algebra $\Lambda = K\mathcal{Q}/I$, we define the algebra associated to \mathcal{L} and Λ to be $\Gamma = \Lambda/(\Lambda e'\Lambda)$, where e' is the sum of the vertices in $\mathcal{Q}_0 \setminus \mathcal{L}_0$. If \mathcal{L} is convex then Λ and Γ have a strong homological connection which we describe. In particular, there is special convex subquiver \mathcal{H} of \mathcal{Q} which we call the homological heart of \mathcal{Q} . We show that if Γ is the algebra associated to \mathcal{H} and Λ , then

- (1) the global dimension of Λ is finite if and only if the global dimension of Γ is finite, and
- (2) the finitistic dimension of Λ is finite if and only if the finitistic dimension of Γ is finite.